

## Overview of UCODE & Associated Codes

### Modes that can be accomplished:

Forward Process Model run with Residuals

Conduct Sensitivity Analysis

Estimate Optimal Parameter values and associated linear uncertainty

Evaluate quality of the model

Estimate values of Predictions and associated linear uncertainty

Evaluate model linearity

Evaluate NonLinear uncertainty associated with estimates of parameter values and predicted values

Auxiliary: Investigate Objective Function

See UCODE Manual

Chapter 1 for overview and description of manual contents

Chapter 2 for overview and program control

Also Chapter 4 Table 3

### Evaluate MODEL LINEARITY - Beale's Measure

Use of linear confidence intervals, assumes the model is linear in the confidence regions of the parameters, this can be tested using Beale's Measure

Sets of parameter values near the optimal values but deviating based on the variances/covariances are generated and used in 2 ways:

To calculate the simulated equivalents using the application codes

achieving convergence for these values may require loosening up solver tolerance log transforming parameters may be necessary to prevent physically impossible negative values

To calculate the simulated equivalents using a linear approximation based on the sensitivities

Given these values Beale's Measure is calculated as:

### Beale's Measure

$$\hat{N}_b = \frac{\sum_{j=1}^{2 \times NP'} \sum_{i=1}^{ND} (\tilde{y}_{ji} - \tilde{y}_{ji}^0) \omega_i (\tilde{y}_{ji} - \tilde{y}_{ji}^0)}{\sum_{j=1}^{2 \times NP'} \sum_{i=1}^{ND} (\tilde{y}_{ji}^0 - \hat{y}_i) \omega_i (\tilde{y}_{ji}^0 - \hat{y}_i)}$$

ND is the number of observations of hydraulic head and flow

$\hat{y}_i$  are hydraulic heads and flows simulated using the optimized parameter values

for the generated sets of values:

$\tilde{y}_{ji}$  represents the values calculated by the application codes

$\tilde{y}_{ji}^0$  represents the calculated linear approximation

**CAUTION:** if a model is optimized using only heads, Beale's measure will not reflect linearity with respect to a flow prediction, which is relevant to validity of the calculation of confidence intervals in the predicted flow

Sets of parameters for calculating **Beale's Measure** are determined based on their variance which depends on their sensitivity and the goodness of fit:

$$\underline{b} = \hat{\underline{b}} \pm \frac{\sqrt{NP} F_{\alpha}(NP, NDOF)}{S_{b_i}} \underline{V}_{b_i}$$

$\hat{\underline{b}}$  = optimal parameter values

$\underline{V}_{b_i}$  = the  $i^{\text{th}}$  column of  $\underline{V}_{b_i} = (\underline{X}^T \omega \underline{X})^{-1} s^2$

$$S_{b_i} = \sqrt{V_{b_{ii}}}$$

Evaluate **MODEL LINEARITY** with **UCODE** (p35 p168)  
ucode3-linearity with **output files from the regression**  
ucode1 **be copied into that folder**

This next step requires only a small change to UCODE input  
that was used for REGRESSION input not PREDICTION input

#### **UCODE\_DATA\_CONTROL**

(linearity=yes) for an execution that does not overwrite any  
previously created output files but needs to have them in the  
directory.

UCODE calculates the simulated equivalents for the  
parameter sets in **\_b1** and writes them in **\_b2**

output: **fn.#umodlin** and **fn.\_b2**

Notice that the parameter sets in **\_b1** are so divers that modflow  
cannot run, so at this point the linearity assessment is beyond our  
reach.

We will resolve that in the future by incorporating transient data

After that is done we would run a UCODE auxiliary code:  
**model\_linearity.exe** (make a batch file for this, p35)

It must be executed in the directory where the files from the  
regression, optimize=yes

And the  
\_b2 file from the linearity=yes  
executions reside.

See **fn.#modlin**, particular comments at the end of the file