



**Given:**

Wet Bulk Density = 2.24 g/cm<sup>3</sup>  
Particle Density = 2.65 g/cm<sup>3</sup>  
Fluid Density (FD) = 1.0 g/cm<sup>3</sup>

**What is:**  
Porosity = ?

$$BD = (1 - \phi) PD + \phi (FD)$$

$$\phi = \frac{SW - DW}{V_T}$$

$$\frac{DW}{V_T} = PD(1 - \phi)$$

$$\phi = 1 - \frac{DW}{PD * V_T}$$

$$BD = (1 - \phi) PD + \phi (FD)$$

$$BD = PD - \phi PD + \phi FD$$

$$BD = PD + \phi (FD - PD)$$

$$BD - PD = \phi (FD - PD)$$

$$\frac{BD - PD}{(FD - PD)} = \phi$$

We have wet bulk density so  $\frac{2.24 - 2.65}{1 - 2.65} = \frac{-0.41}{-1.65} \sim 0.25 = \phi$   
use fluid density for water



**Knowing:**

Wet Bulk Density = 2.24 g/cm<sup>3</sup>  
Particle Density = 2.65 g/cm<sup>3</sup>  
Fluid Density (FD) = 1.0 g/cm<sup>3</sup>  
Porosity = 0.25

**And If:**

Total Volume = 25cm<sup>3</sup>

**What is:**

Saturated Weight = ?

Dry Weight = ?

$$BD = (1 - \phi) PD + \phi (FD)$$

$$\phi = \frac{SW - DW}{V_T}$$


$$\frac{DW}{V_T} = PD(1 - \phi)$$

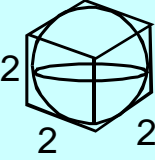
$$\phi = 1 - \frac{DW}{PD * V_T}$$

Saturated "Weight" = Vol \* WBD = 25cm<sup>3</sup> \* 2.24  $\frac{g}{cm^3}$  = 56g (MASS)

Dry Weight = SatWgt - WaterWgt = SatWgt -  $\phi$  TotVol \* FD

= 56g - (0.25\*25cm<sup>3</sup>) \* 1  $\frac{g}{cm^3}$  = 56g - 6.25g = 49.75g ~ 50g (MASS)



$$\phi = \frac{V_V}{V_T} = \frac{2^3 - \left(m \frac{4}{3} \pi r^3\right)}{2^3}$$


m is # spheres    r is their radius


m	r	r <sup>3</sup>	mr <sup>3</sup>
1	1	1	1
8	1/2	1/8	1
64	1/4	1/64	1

$$\phi = \frac{2^3 - \left(\frac{4}{3} \pi\right)(1)}{2^3} = 0.476 \quad \text{A constant!}$$

**HENCE MAX  $\phi$  FOR UNIFORM, CUBIC PACKED SPHERES IS ~ 48%**

**MIN  $\phi$  WOULD RESULT FROM RHOMBEHEDRAL PACKING ~ 26%**

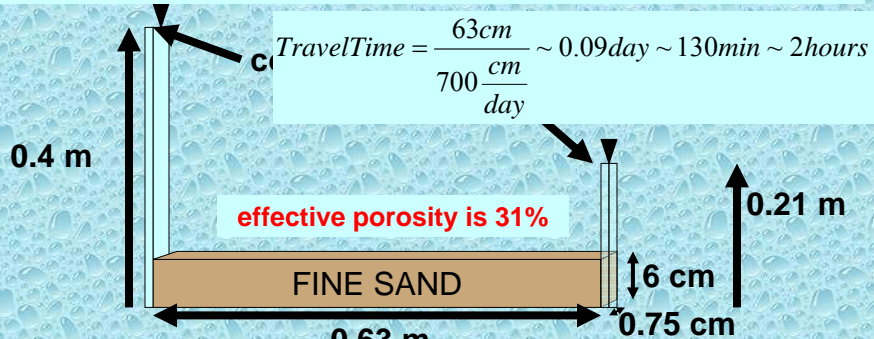
**IN GENERAL, IRREGULAR PACKING & ANGULAR PARTICLES YIELD HIGHER  $\phi$**



$$Q = \frac{1 \text{ liter}}{\text{day}} = \frac{1 \text{ liter}}{\text{day}} \frac{1000 \text{ cm}^3}{1 \text{ liter}} = \frac{1000 \text{ cm}^3}{\text{day}}$$

$$\text{Darcy Velocity} = \frac{Q}{\text{Area}} = \frac{1000 \text{ cm}^3}{6 \text{ cm} \cdot 0.75 \text{ cm}} = 222 \frac{\text{cm}}{\text{day}}$$

$$\text{Average Linear Velocity} = \frac{\text{Darcy Velocity}}{\text{Effective Porosity}} = \frac{222 \frac{\text{cm}}{\text{day}}}{0.31} = 716 \frac{\text{cm}}{\text{day}} \sim 700 \frac{\text{cm}}{\text{day}}$$

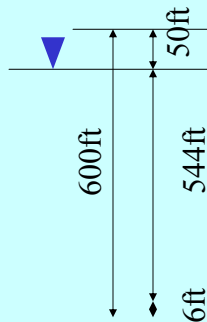
$$\text{Travel Time} = \frac{63 \text{ cm}}{700 \frac{\text{cm}}{\text{day}}} \sim 0.09 \text{ day} \sim 130 \text{ min} \sim 2 \text{ hours}$$


**effective porosity is 31%**

**FINE SAND**



**pressure on your head (6ft tall) at the bottom of a well  
surface at sea level  
bottom at 600 ft  
water level 50 ft below the surface**



Gage Pressure

$$P = \gamma h = 62.4 \frac{lb}{ft^3} 544 ft = 33945.6 \frac{lb}{ft^2}$$

$$P = 33945.6 \frac{lb}{ft^2} \frac{1}{144} \frac{ft^2}{in^2}$$

$$= 235.7 \frac{lb}{in^2} = 235.7 psi$$

Absolute Pressure ~ 235.7psi + 14.7psi  
~ 250.4psi

**Surface tension for distilled water in contact with air in a clean  
glass tube is 72.8 dynes/cm**

1 dyne: imparts an acceleration of 1 cm/sec/sec to a mass of 1 gram

$$\sigma = \frac{72.8 \text{ dyne}}{\text{cm}} \left[ \frac{0.00102 \text{ g}_f}{\text{dyne}} \frac{981 \text{ cm}}{\text{sec}^2} \right] = \frac{72.8 \text{ g}}{\text{s}^2}$$

$$\gamma = \rho g = \frac{1 \text{ g}}{\text{cm}^3} \frac{980 \text{ cm}}{\text{s}^2} = \frac{980 \text{ g}}{\text{cm}^2 - \text{s}^2}$$

$$h_c = \frac{2\sigma}{\gamma r} = \frac{2 \frac{72.8 \text{ g}}{\text{s}^2}}{\frac{980 \text{ g}}{\text{cm}^2 - \text{s}^2} r} \approx \frac{0.15}{r} \text{ cm (for } r \text{ in cm)}$$



Use  $d_{10}$  to reflect the typical pore throat size

For fresh water:

$$h_c = \frac{2\sigma}{\gamma r} \quad (\text{for } r \text{ in cm})$$

$$\sigma = \frac{72.8 \text{ dyne}}{\text{cm}} \frac{0.00102 \text{ g}}{\text{dyne}} \frac{981 \text{ cm}}{\text{sec}^2} = \frac{72.8 \text{ g}}{\text{s}^2}$$

$$\gamma = \rho g = \frac{1 \text{ g}}{\text{cm}^3} \frac{980 \text{ cm}}{\text{s}^2} = \frac{980 \text{ g}}{\text{cm}^2 \text{ s}^2}$$

For sand

$$h_{c\text{-water}} = (2 \cdot 72.8) / (980 \cdot 0.017 / 2) = 17.5 \text{ cm}$$

$$h_{c\text{-gas}} = (2 \cdot 33) / (0.68 \cdot 980 \cdot 0.017 / 2) = 11.6 \text{ cm}$$

For silty-sand

$$h_{c\text{-water}} = (2 \cdot 72.8) / (980 \cdot 0.0017 / 2) = 174 \text{ cm}$$

$$h_{c\text{-gas}} = (2 \cdot 33) / (0.68 \cdot 980 \cdot 0.0017 / 2) = 116 \text{ cm}$$