# Overview of UCODE & Associated Codes Modes that can be accomplished:

Forward Process Model run with Residuals

Conduct Sensitivity Analysis

Estimate Optimal Parameter values and associated linear uncertainty

Evaluate quality of the model

Estimate values of Predictions and associated linear uncertainty

Evaluate model linearity

Evaluate NonLinear uncertainty associated with estimates of parameter values and predicted values

Auxiliary: Investigate Objective Function

See UCODE Manual Chapter 1 for overview and description of manual contents

When prediction=yes, UCODE calculates predictions and sensitivities (if sensitivities=yes) of the model parameters to those predicted values for the purpose of calculating 95-percent linear confidence and prediction intervals on the predictions. IN PREDICTION MODE WE CHANGE THE PROCESS MODEL TO THE PREDICTIVE CONDITIONS

We will get both
CONFIDENCE INTERVALS and PREDICTION INTERVALS
ON PREDICTED VALUES

CONFIDENCE INTERVALS are based on var-cov of parameters, reflecting certainty associated with the parameters

PREDICTION INTERVALS are based on var-cov of parameters AND the measurement error reflecting our ability to measure the predicted value

## 3 ALTERNATIVE METHODS OF CALCULATION OF INTERVALS for both CONFIDENCE INTERVALS AND PREDICTION INTERVALS on PREDICTIONS

Appropriate method depends on # of predictions jointly considered

- 1) INDIVIDUAL INTERVALS
- 2) SIMULTANEOUS INTERVALS more than one interval
- 3) SIMULTANEOUS INTERVALS undefined number of intervals (e.g. drawdown over an area must be limited to a given magnitude, but the location of the maximum drawdown cannot be determined a priori).

Only the critical values differ and are obtained from one of:

Student-t Distribution

Bonferroni-t Distribution

Scheffe (based on the F-distribution)

UCODE tests for the appropriate method, then prints intervals for Individual and Both Simultaneous Intervals. Of these 3, the user selects the interval appropriate for their question.

#### INDIVIDUAL CONFIDENCE INTERVALS

$$z_{\ell} \pm t_{s} \left(n, 1.0 - \frac{\alpha}{2}\right) s_{\ell}$$

 $\mathbf{z}_{\ell}^{'}=\ell^{\text{th}}$  simulated value

Sensitivity of the simulated equivalent of the prediction to the parameters

$$t_s\left(n, 1.0 - \frac{\alpha}{2}\right) = \text{critical value, value with } \frac{\alpha}{2} \text{ probability that}$$

a student-t distributel random value wouldbe larger

n = degreesof freedom(ND + NPR - NP)

 $\alpha = significance level, commonly 0.05 or 0.10 (5 or 10%)$ 

 $s_{x'}$  = standard deviation of the prediction

$$s_{z'} = \begin{bmatrix} NP & NP & \\ \sum_{i=1}^{NP} & \frac{\partial z'}{\partial b_i} \end{bmatrix} V(b_{ij}) \begin{bmatrix} \frac{1}{2} & \\ \frac{\partial z'}{\partial b_i} \end{bmatrix}$$
Element ij of the variance/covariance matrix

#### SIMULTANEOUS CONFIDENCE INTERVALS

Two Methods: Bonferroni & Scheffe

Both conservative with respect to significance level Both are calculated by UCODE and the smaller is used

Bonferroni:  $z_z \pm t_B \left( n, 1.0 - \frac{\alpha}{2k} \right) s_z$ 

where k is the number of simultaneous intervals and  $\mathbf{t}_{\mathrm{B}}$  is the Bonferroni - t probability distribution for a

given number of degrees of freedom and

simultaneo us intervals

at the selected significance level

Scheffe:  $z_{\ell}^{'} \pm t_{s}(d, F_{\alpha}(d, n)) s_{r'}$ 

where d = k (# simultaneous intervals)

OR

the # of parameters (which everis less) and

 $F_\alpha$  is the critical value from the F probability distribution for a given number of degreesof freedom at the

selectedsignifican ce level

PREDICTION INTERVALS are broader than confidence intervals because they include the probability that the MEASURED value will fall into the interval. Calculations are the same as for confidence intervals, however the standard deviation is increased to reflect the measurement error as follows:

$$z_{z}^{'} \pm t_{s} \left( n, 1.0 - \frac{\alpha}{2} \right) \left( s_{z_{z}^{'}} + s_{a} \right)$$

where  $\mathbf{s_a}$  is the product of the standard error of the regression and the expected measurement error of the prediction

### EVALUATE PREDICTIVE UNCERTAINTY using OPTIMAL PARAMETER VALUES with UCODE

Develop a predictive MODLFOW Model

Import to ModelMate as per instructions in PDF file

Run UCODE with prediction=yes, first to be sure all is functioning correctly

Then with sensitivity=yes

UCODE calculates the sensitivity of the predictions to the parameters at the optimal values

linear\_uncertainty is executed in that folder with the ucode root file name as input, e.g.

C:\WRDAPP\UCODE\_2005\bin\linear\_uncertainty.exe ep\_Ucode

This ucode prediction execution must be done in the folder with the regression data exchange files and does not overwrite previously created UCODE output files

It produces additional files

```
#upred
_p _pv _dmp _spu _sppp _sppr _spsp _spsr
```

The linear\_uncertainty execution produces

```
#linunc and ._linp
```

You can view the results in GW\_Chart